A scenic view of a traditional Chinese garden. In the foreground, a pond is filled with lily pads. In the middle ground, there is a large, dark wooden pavilion with a multi-tiered roof. In the background, another smaller pavilion is visible, surrounded by lush green trees. The sky is clear and blue.

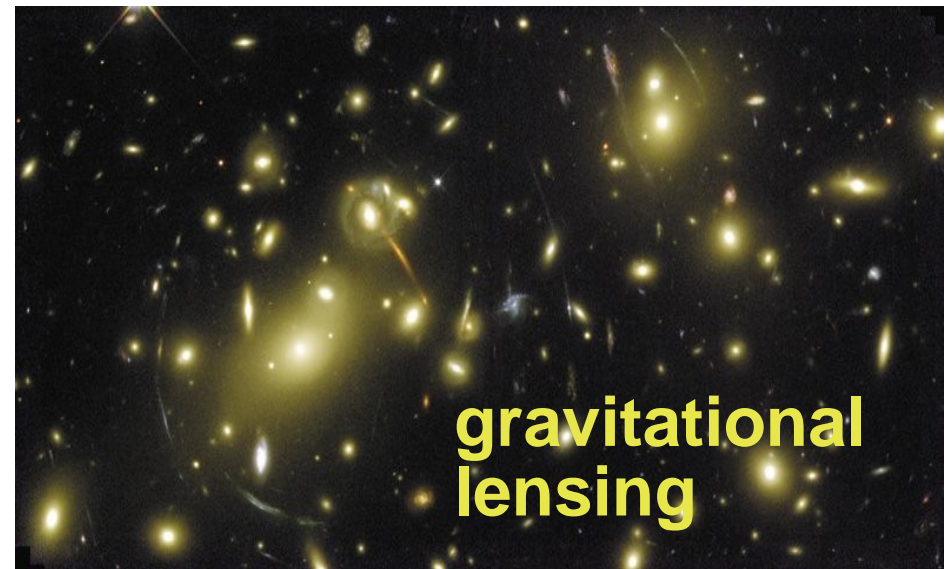
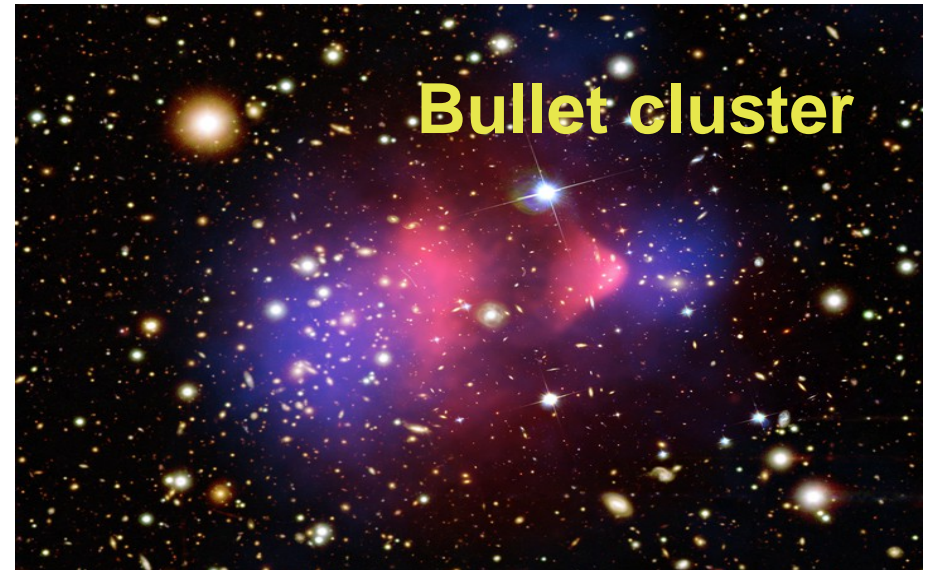
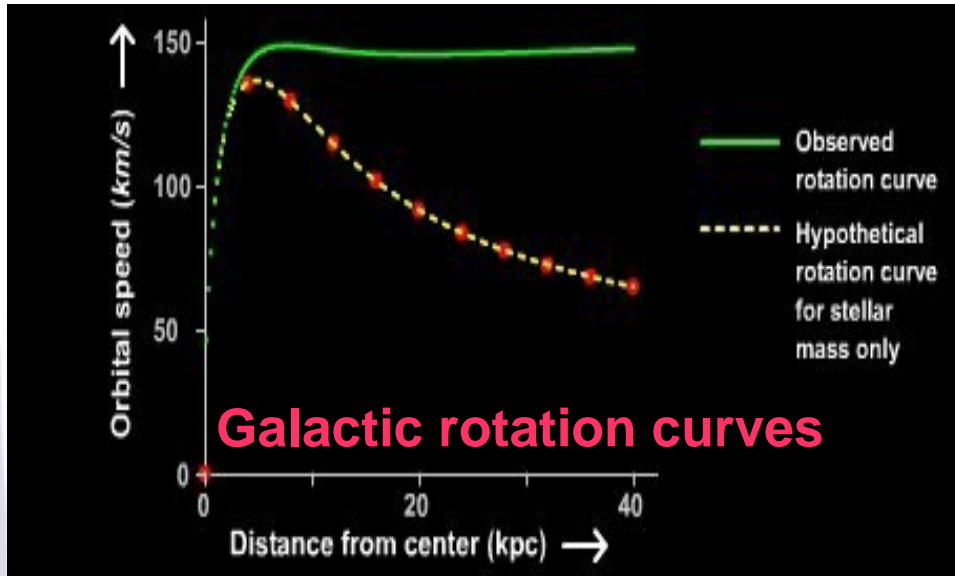
SUSY and alike Mass Measurements @ LHC

Partha Konar

*Physical Research Laboratory
Ahmedabad*

The 4th KIAS Workshop
on Particle Physics and Cosmology

Evidence of Dark Matter

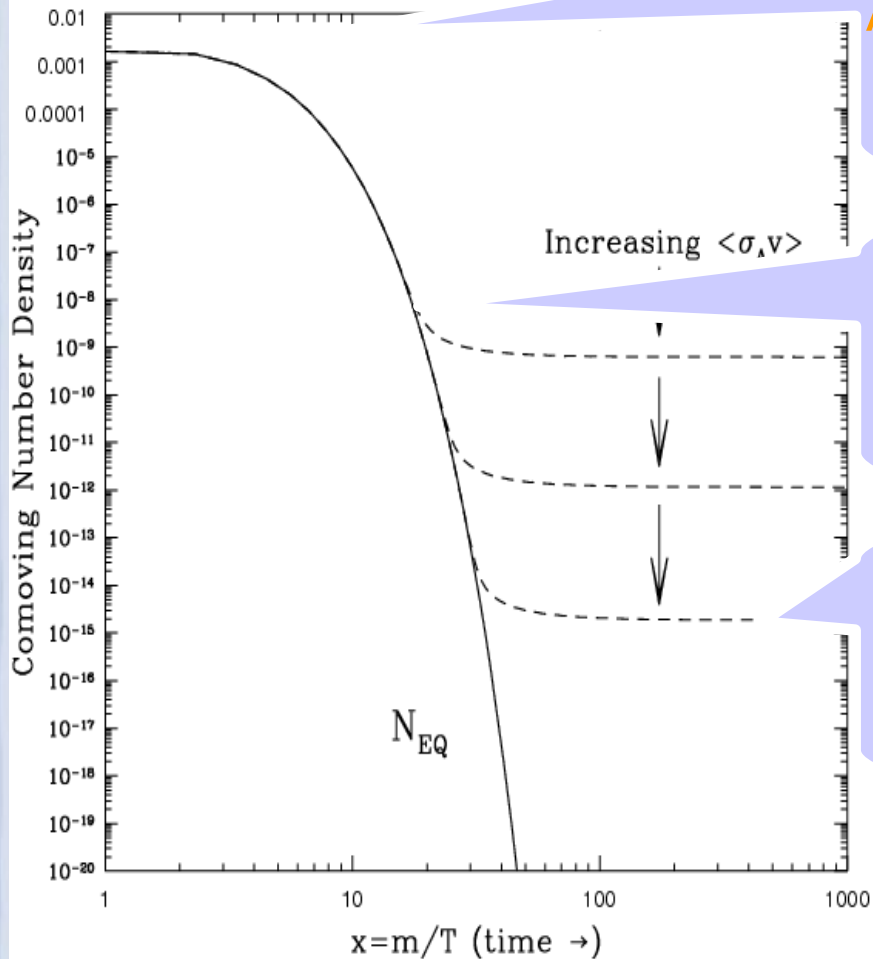


What could dark matter be?

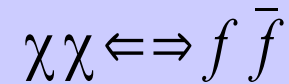
- ✓ Something **MASSIVE** (cold DM)
- ✓ Interacts via the **weak interaction**
- ✓ Something different from our known Particles!
- **WIMPS** : Weakly Interacting Massive Particles

*Not normal matter at all, but
something entirely exotic and unknown*

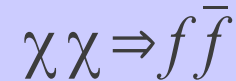
Thermal history of WIMP



A new (heavy) particle χ in Thermal equilibrium



Universe cooling down



χ freeze out



Relic abundance

$$\Omega_{DM} \propto \frac{1}{\sigma_{an}}$$

WIMP miracle or coincidence?

Observed value for the Dark Matter density

$$\Omega_{DM}^{cosmos}$$

$$\Omega_{CDM} h^2 = 0.110 \pm 0.006$$



$$\Omega_{DM}^{wimp}$$

$$\simeq 0.1 \times \left(\frac{3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma v \rangle} \right)$$

New physics at weak scale?

$$\langle \sigma v \rangle \simeq 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

- Cosmology indicates to explore at weak scale
- BSM independently predicts particle with right density as DM!
- Evidence of new physics? Driving motivation for DM search.

Theoretical Wimp density at "freeze-out"

Dark Matter

Cosmology vs Missing particles at Collider

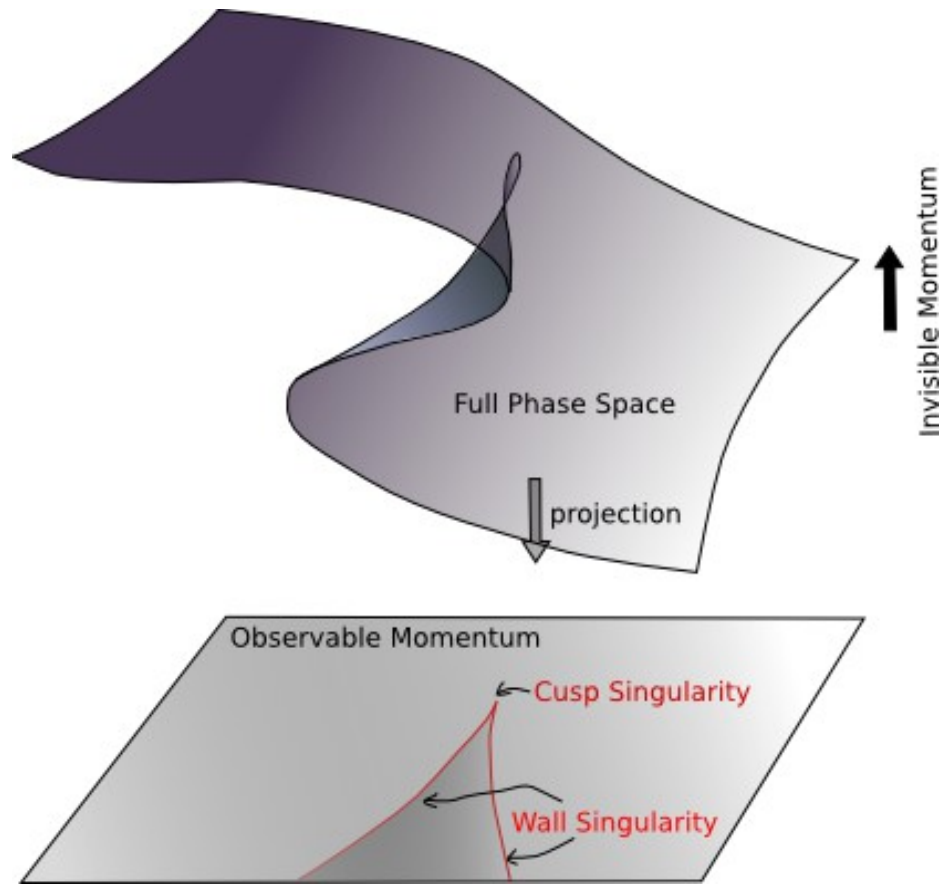
Cosmic Relic Density : $\Omega_\chi h^2 \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_\chi^2}{\alpha^2}$

- Crossing: $\chi\chi$ production \sim annihilation \sim scattering.

---- are they same??

- SM – Neutrino
- BSM – 'Dark matter' at the laboratory
- P_T^{miss} signature at LHC + DM motivated models:
Difficult to fully reconstruct events and extract masses, couplings of new particles.

Mass measurements : Behind the curtain



- *Global approach:*
Determine the mass scale of new physics.
- *After NP discovery:*
Look for specific topology typically with (long) decay chain. Isolate them to extract mass informations.

Singularities in observable phase space?
→ end-point, cusp, kink...

Mass measurements : recollection

Mass scale of new physics (No trial mass parameters)

- Transverse variables - E_T, H_T, M_{eff}
- Global inclusive variables - $E, M, M_{Tgen}^{max}, \hat{S}_{min}$

Specific topology + extract mass informations :

- Invariant mass endpoint boundary line
- Polynomial method
- Transverse mass variables and variants:

$$M_{T2}, M_{CT}, M_{T2}(n, c, p), M_{T2}(perp), M_2$$

- Hybrid method

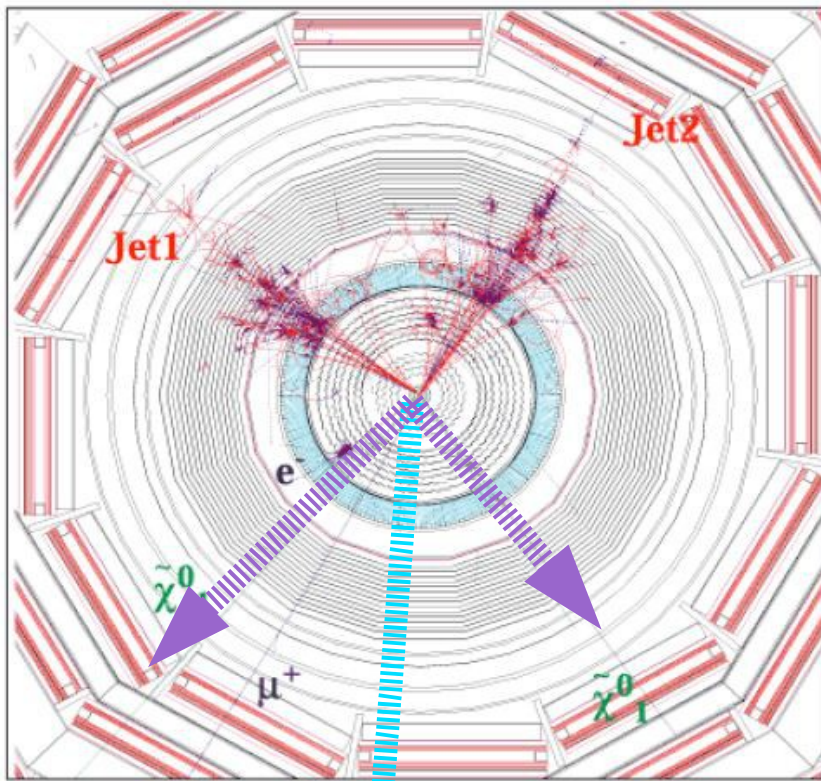
Hinchliffe, Paige, Bachacou, Allanach, Lester, Parker, Webber, Gjelsten, Miller, Osland ..

Nojiri, Polesello, Tovey, Cheng, Gunion, Han, McElrath, Marandella ..

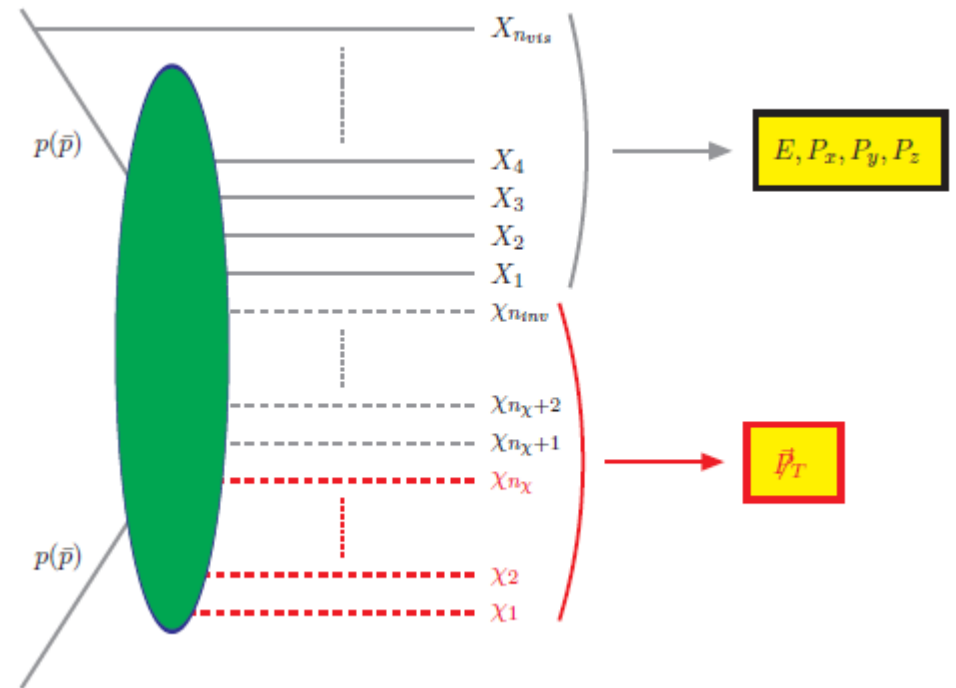
Lester, Summers, Barr, Stephens, Tovey, Cho, Choi, Kim, Park, Kong, Matchev, Park, Burn ..

P_T^{miss}

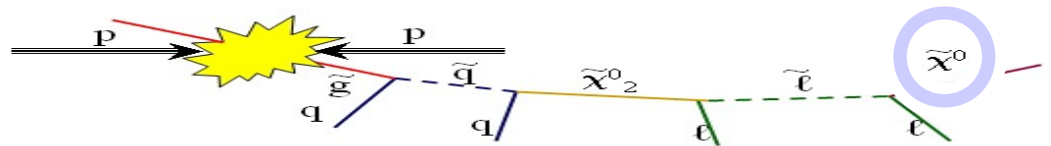
Events @ LHC: Different viewpoint



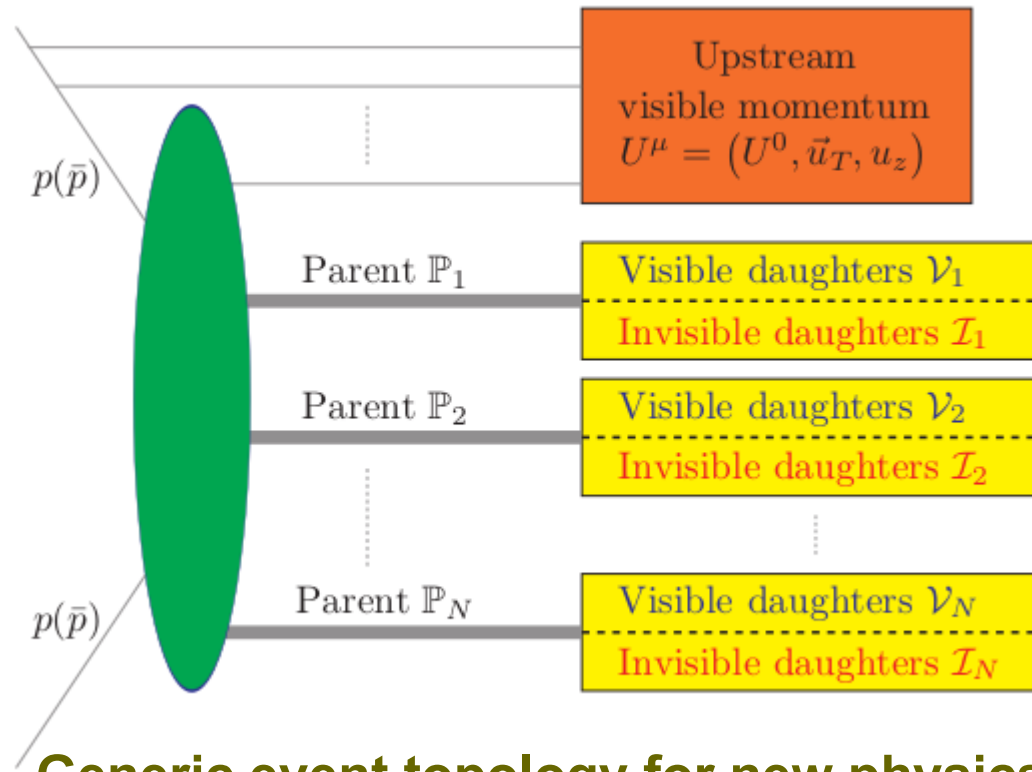
Missing P_T



Dark matter candidate



Event Partitioning



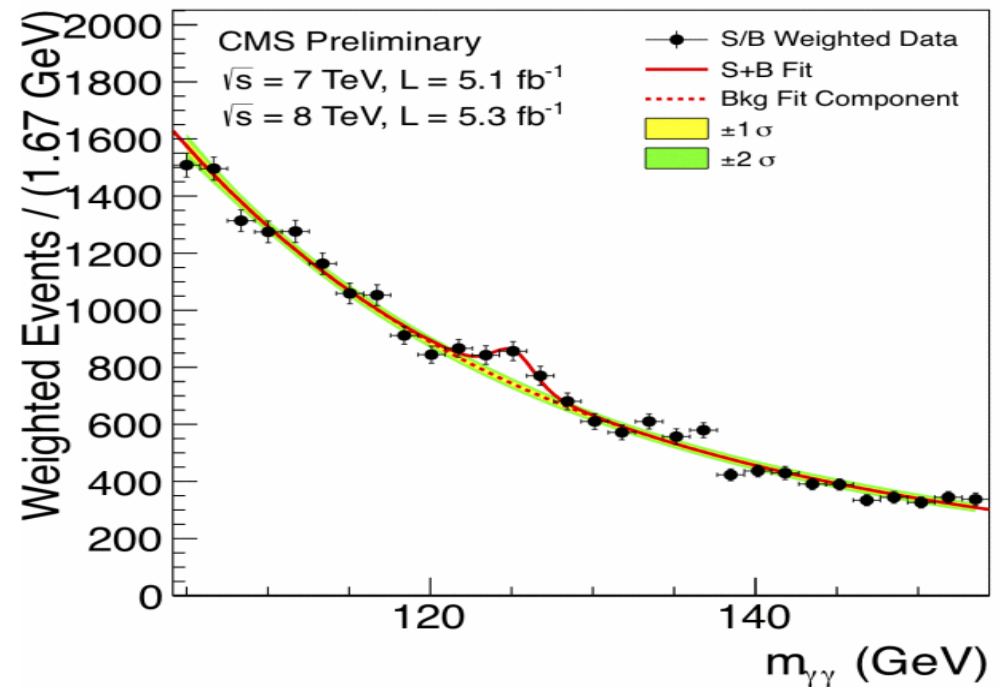
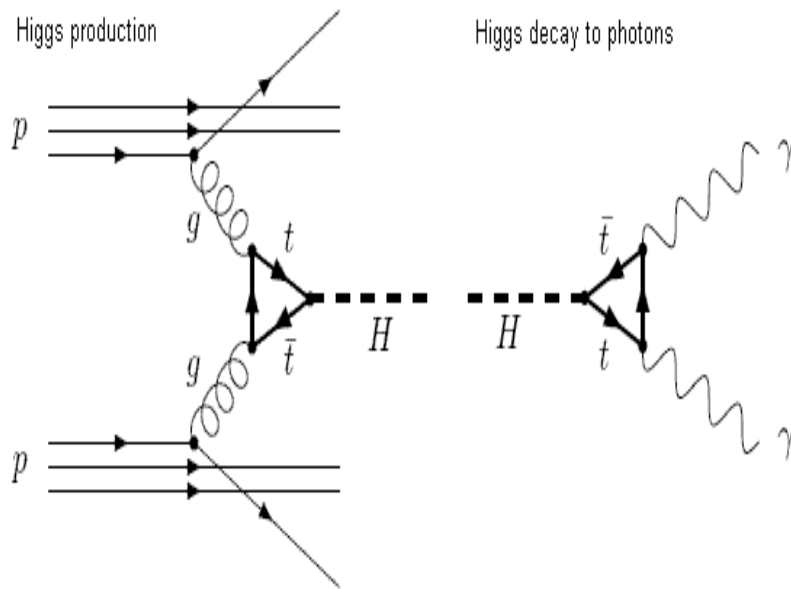
Generic event topology for new physics

**Constraint in
Transverse Projection**

$$\sum_{i=1}^{N_{\mathcal{I}}} \vec{q}_{iT} = \vec{p}_T^\# \equiv -\vec{u}_T - \sum_{i=1}^{N_{\mathcal{V}}} \vec{p}_{iT}.$$

★ Z or h – mass measurements

The “Standard signals”: **All visible decay**



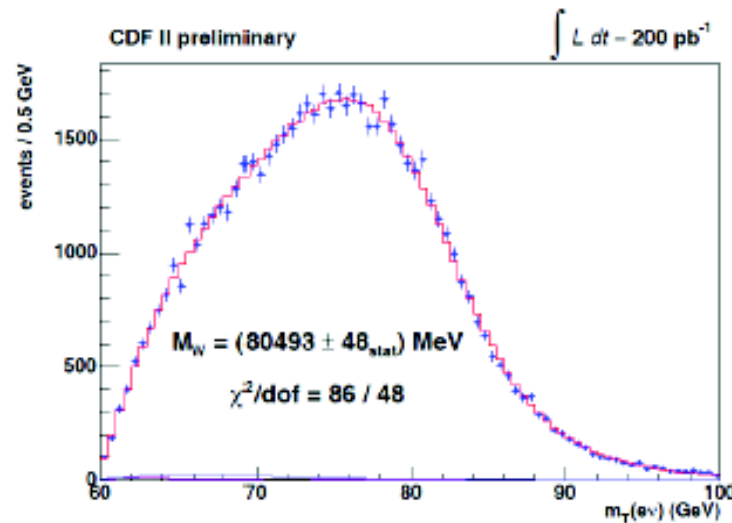
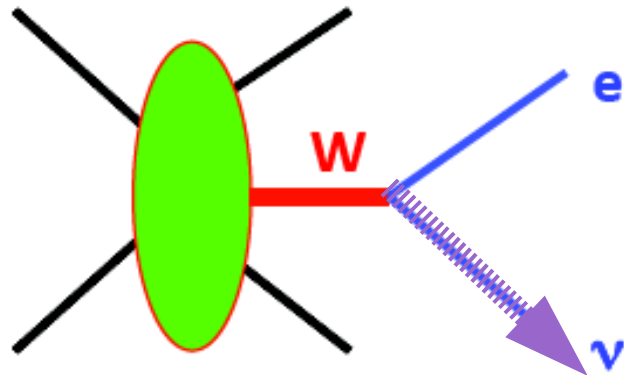
Invariant Mass (M)

$$M_h^2 = M^2(\gamma, \gamma) \equiv (|\vec{P}_1| + |\vec{p}_2|)^2 - (\vec{P}_1 + \vec{p}_2)^2$$



W – mass measurements

The “Standard signals”: **single Semi-invisible decay**



Transverse Mass (MT)

~ massless neutrino

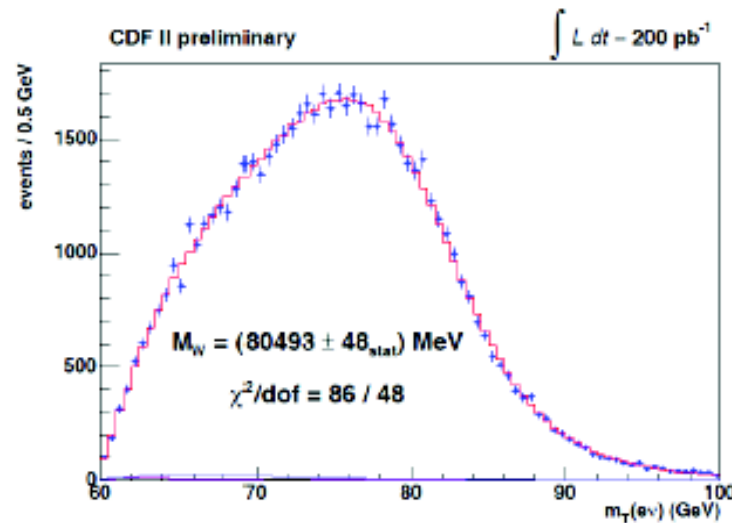
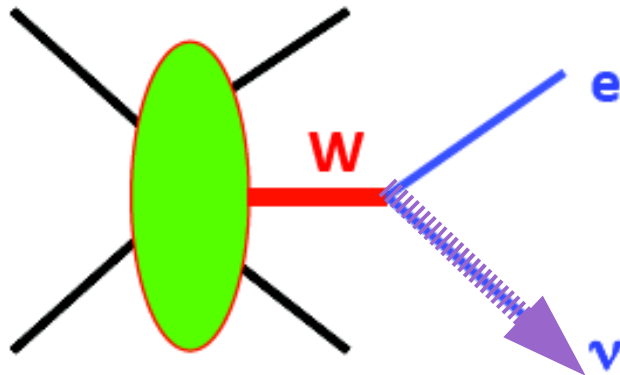
$$M_w^2 \geq M_T^2(l, \nu) \equiv (|\vec{P}_T^l| + |\vec{q}_T^\nu|)^2 - (\vec{P}_T^l + \vec{q}_T^\nu)^2$$

Kinematic end point over many points



W – mass measurements

The “Standard signals”: **single Semi-invisible decay**



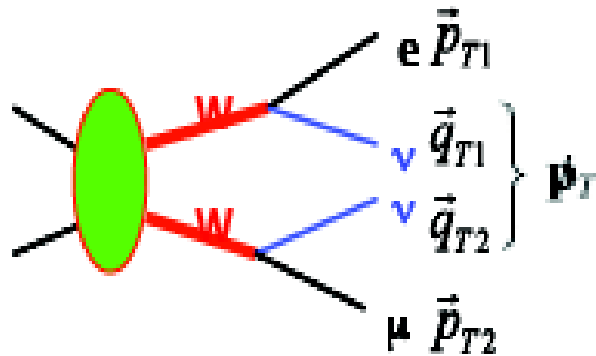
Transverse Mass (MT)

~ massless neutrino

$$M_w^2 \geq M_T^2(l, \nu) \equiv (|\vec{P}_T^l| + |\vec{q}_T^\nu|)^2 - (\vec{P}_T^l + \vec{q}_T^\nu)^2$$

Kinematic end point over many points

If there are **two** invisibles?



$$M_T \longrightarrow M_{T2}$$

- If we could have measured q's!
- For each leg $M_W^2 \geq M_T^2(l, \nu) \equiv (|\vec{P}_T^l| + |\vec{q}_T^\nu|)^2 - (\vec{P}_T^l + \vec{q}_T^\nu)^2$

$$M_W \geq \max\{m_T(\vec{p}_{T1}, \vec{q}_{T1}), m_T(\vec{p}_{T2}, \vec{q}_{T2})\}$$

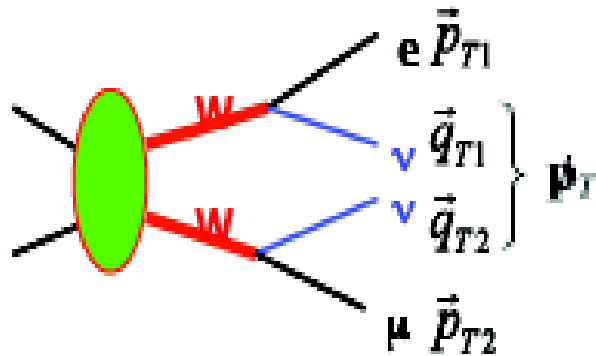
- Without having transverse momentum of each missing one:

$$M_W \geq M_{T2} = \min_{\vec{q}_{T1} + \vec{q}_{T2} = \vec{E}_T} [\max\{m_T(\vec{p}_{T1}, \vec{q}_{T1}), m_T(\vec{p}_{T2}, \vec{q}_{T2})\}]$$

- Minimization over all possible 'trial' q-momentum.

Lester, Summers, Barr..

If there are **two** of them?



- If we could measure q's!
- For each leg $M_w^2 \geq M_T^2(l, \nu) \equiv (|\vec{P}_T^l| + |\vec{q}_T^\nu|)^2 - (\vec{P}_T^l + \vec{q}_T^\nu)^2$

$$M_w \geq \max\{m_T(\vec{p}_{T1}, \vec{q}_{T1}), m_T(\vec{p}_{T2}, \vec{q}_{T2})\}$$

- Without having transverse momentum of each missing one:

$$M_T \longrightarrow M_{T2}$$

$$M_w \geq M_{T2} = \min_{\vec{q}_{T1} + \vec{q}_{T2} = \vec{E}_T} [\max\{m_T(\vec{p}_{T1}, \vec{q}_{T1}), m_T(\vec{p}_{T2}, \vec{q}_{T2})\}]$$

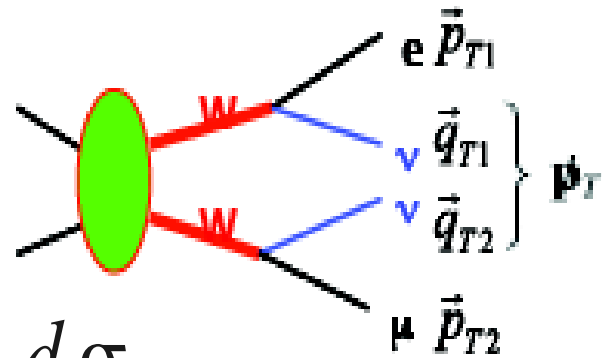
$$M_{T2}^{\max} \rightarrow M_w$$

{Over all events}

- Minimization over all possible 'trial' q-momentum.

Lester, Summers, Barr..

In place of 'neutrinos' something **massive**!!



- Take a trial ν mass $\rightarrow \tilde{m}_0$
- Look for $M_{T2}(\tilde{m}_0)$ distribution

Find $M_{T2}^{max}(\tilde{m}_0)$

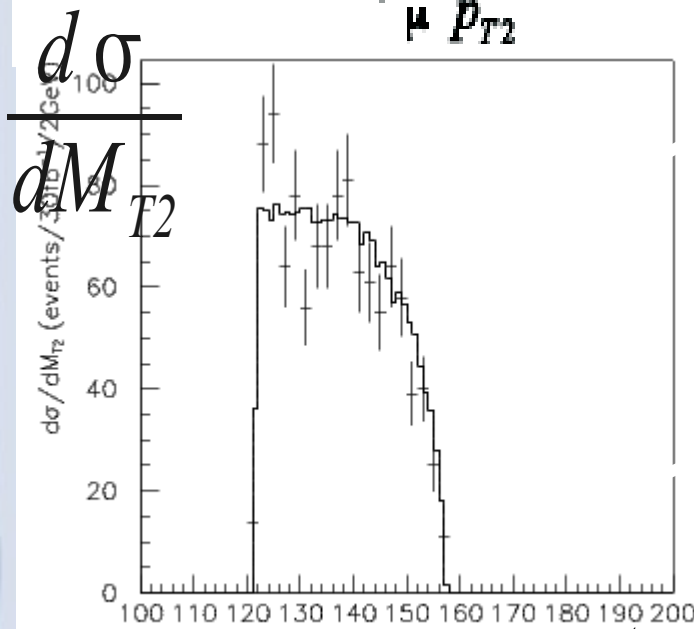
$$pp \rightarrow X + \tilde{l}_R^+ \tilde{l}_R^- \rightarrow X + l^+ l^- \tilde{\chi}_1^0 \tilde{\chi}_1^0$$

$$m_{\tilde{l}_R} = 157.1 \text{ GeV}, \quad m_{\tilde{\chi}_1^0} = 121.5 \text{ GeV}.$$

$$m_{T2}^{max} \simeq 157 \text{ GeV} \rightarrow \tilde{m}_1$$

$$\text{(with } m_{\tilde{\chi}_1^0} = 121.5 \text{ GeV)} \rightarrow \tilde{m}_0$$

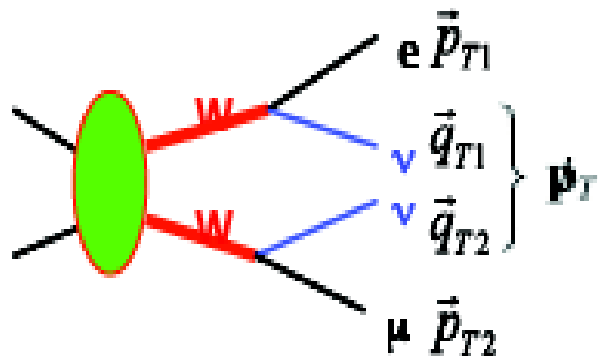
$$M_{T2}(\tilde{m}_0)$$



Lester, Summers'99

If 'neutrinos' were massive!!

- Take a trial ν mass $\rightarrow \tilde{m}_0$
- Look for $M_{T2}(\tilde{m}_0)$ distribution



Find $M_{T2}^{max}(\tilde{m}_0)$

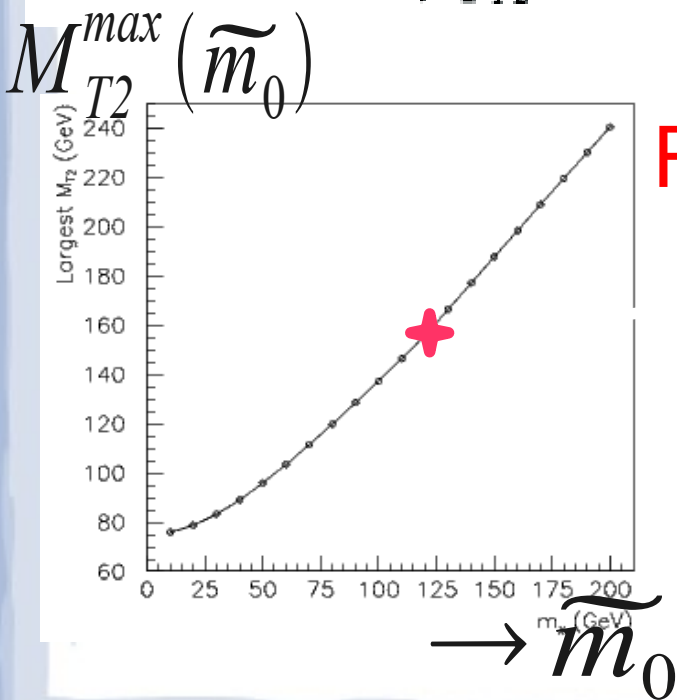
$$pp \rightarrow X + \tilde{l}_R^+ \tilde{l}_R^- \rightarrow X + l^+ l^- \tilde{\chi}_1^0 \tilde{\chi}_1^0$$

Role of trial mass

$$m_{\tilde{l}_R} = 157.1 \text{ GeV}, \quad m_{\tilde{\chi}_1^0} = 121.5 \text{ GeV}.$$

$$m_{T2}^{max} \simeq 157 \text{ GeV} \rightarrow \tilde{m}_1$$

$$(\text{with } m_{\tilde{\chi}_1^0} = 121.5 \text{ GeV}) \rightarrow \tilde{m}_0$$

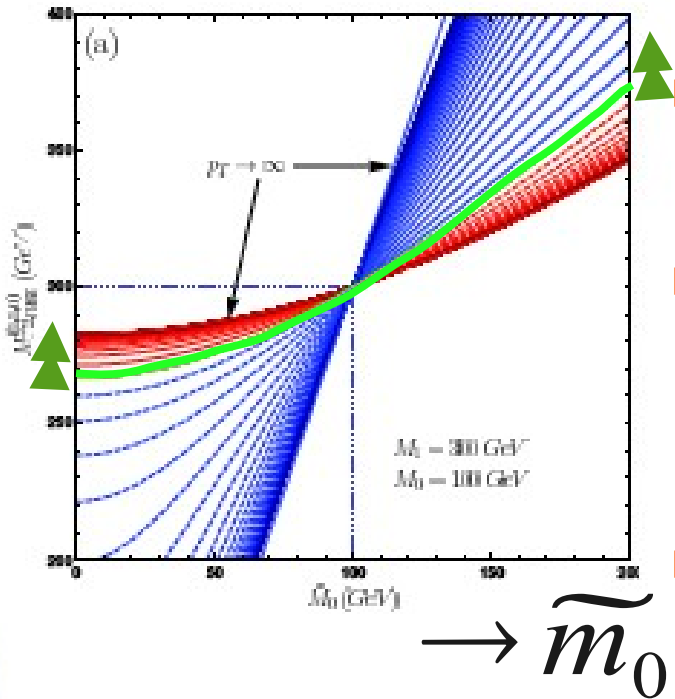


Lester, Summers'99

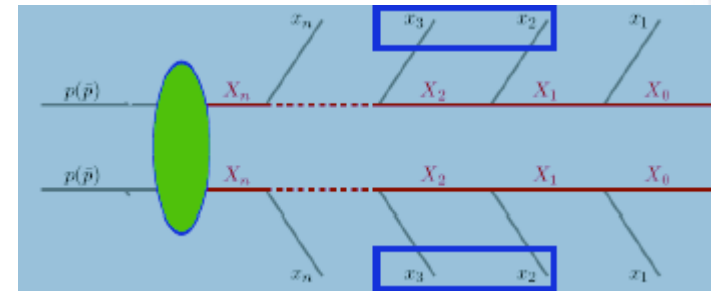
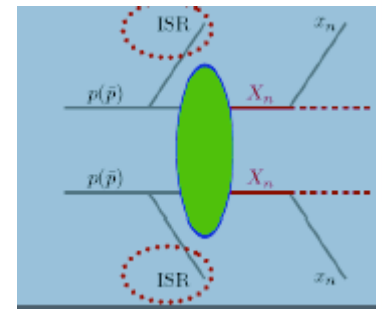
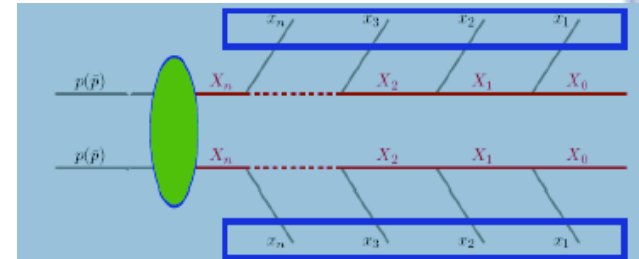
Magic Kink !

- Kink can arise from

$$M_{T2}^{max}(\tilde{m}_0)$$



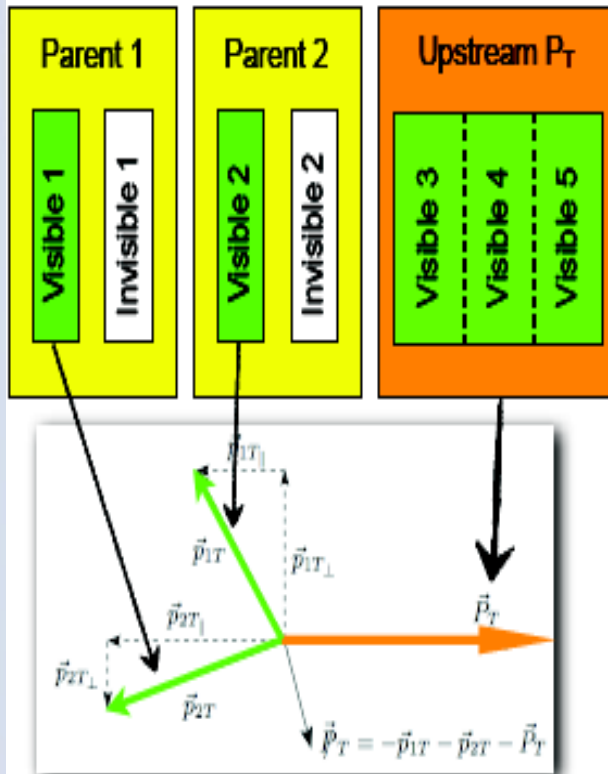
- Composite particle each side
Cho, Choi, Kim, Park '07
- ISR effect
Barr, Gripaos, Lester '07
Burns, Kong, Matchev, Park '08
- Subsystem



Burns, Kong, Matchev, Park'08

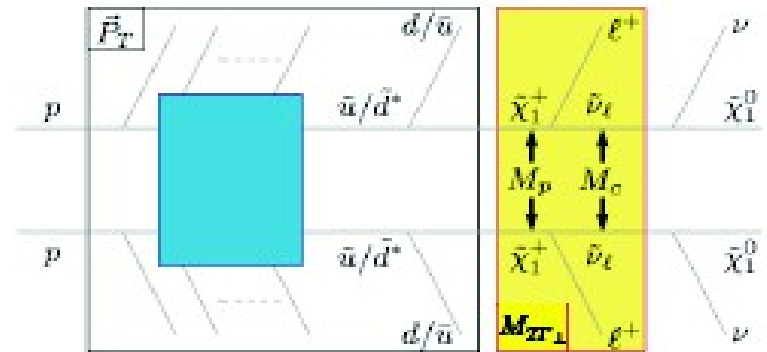
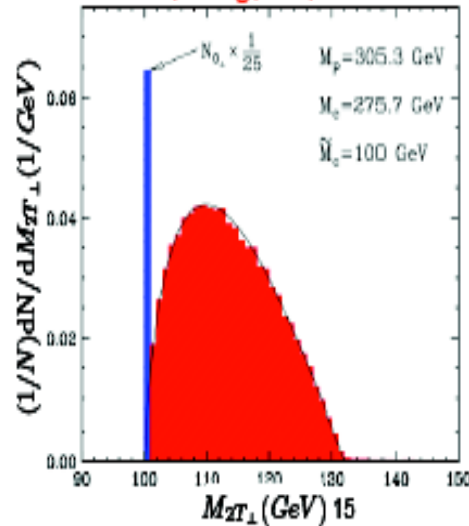
Second Transversification

- Having projected on the transverse plane, one can additionally project on the direction of Upstream P_T :

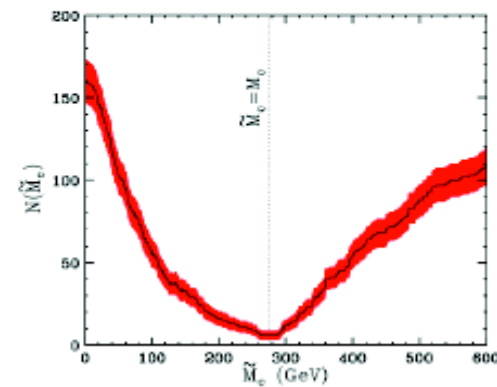


- The endpoints of “perp” distributions are stable against P_T variations

Konar, Kong, KM, Park 2009



$$N(\tilde{M}_c) = \sum_{\text{all events}} H(M_{2T}(\tilde{M}_c) - M_{2T\perp}^{\text{max}}(\tilde{M}_c))$$



pk, Kong, Matchev, Park'09

Global inclusive variables

- Mass scale of new physics.
- Make use of all observed momenta including Z-component, without hypothesising any particular topology or final states.
 - Total visible energy : E
 - Total visible inv. Mass : M
 - Oxbridge variable: M_{Tgen}^{max}
 - Gator variable: $\sqrt{\hat{s}_{min}}$

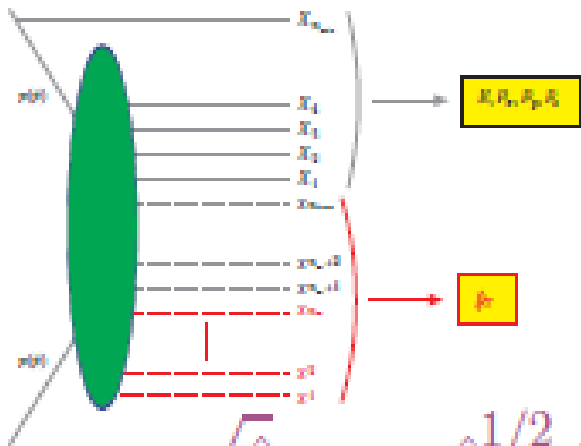
Mass scale measurement

- Depend on both M_{SUSY} and M_χ OR don't!

→ $M_{susy}^{eff} = \left(M_{susy} - \frac{M_\chi^2}{M_{susy}} \right)$ $H_T \equiv E_T + \cancel{E}_T$ $E_T \equiv \sum_\alpha E_\alpha \sin \theta_\alpha$ $M_{eff} = \cancel{E}_T + \sum_{\text{jets } j} p_{Tj}$

→ Oxbridge variant : $m_{Tgen}^{max}(m_\chi) = M_{SUSY}$

→ Gator variable $S_{min}(m_\chi) = (2 M_{SUSY})^2$

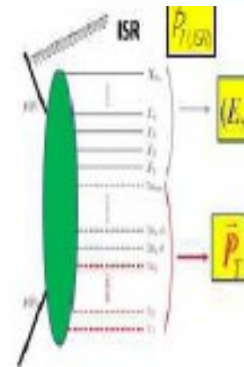


$$\hat{s} = \left(E + \sum_{i=1}^{n_{inv}} \sqrt{m_i^2 + \vec{p}_i^2} \right)^2 - \left(\vec{P} + \sum_{i=1}^{n_{inv}} \vec{p}_i \right)^2$$

Find: The *minimum* value of the Mandelstam variable consistent with the measured values of the *total energy E*, *total visible momentum (Px, Py, Pz)* and *Missing \cancel{E}_T* !

$$\sqrt{\hat{s}_{min}} \equiv \hat{s}_{min}^{1/2}(M_{inv}) = \sqrt{E^2 - P_z^2} + \sqrt{\cancel{E}_T^2 + M_{inv}^2}$$

$\sqrt{\hat{s}_{min}}$: Subsystem



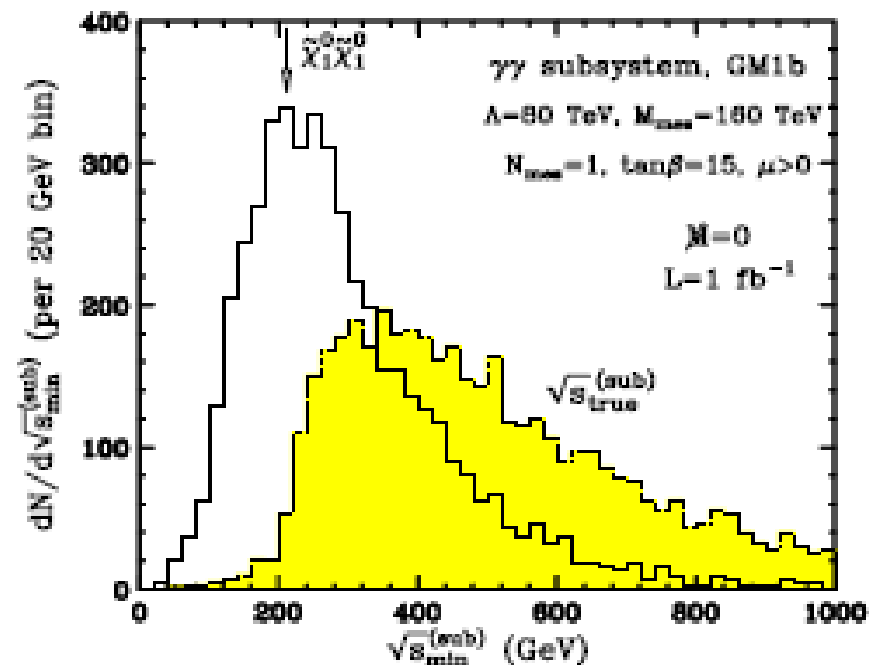
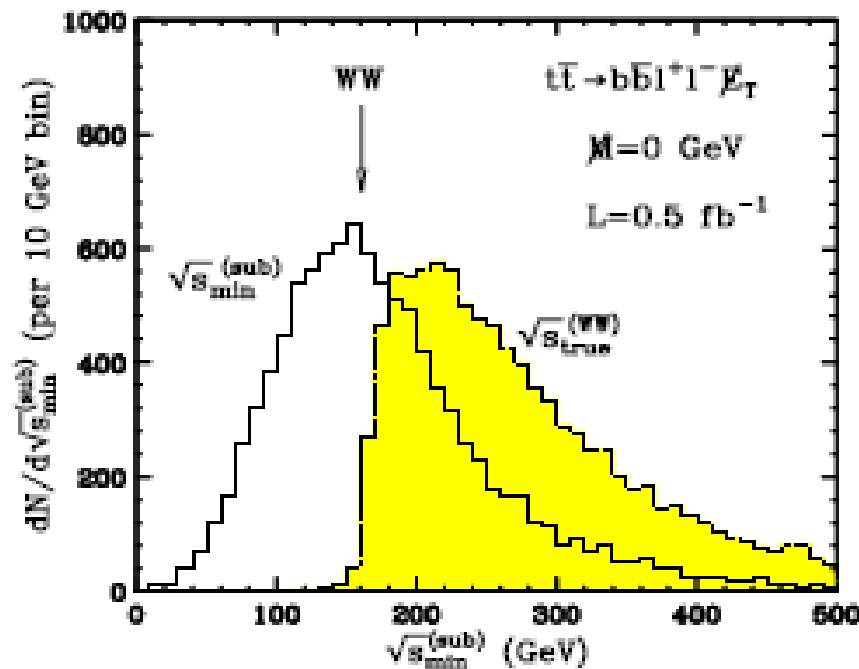
$$\sqrt{\hat{s}_{min}} = \sqrt{(\sqrt{E^2 - P_z^2} + \sqrt{P_T^2 + M_{inv}^2})^2 - P_{T(ISR)}^2}$$

- tt-bar events**

- identify the WW threshold from the 2 lepton subsystem

- GMSB SUSY events**

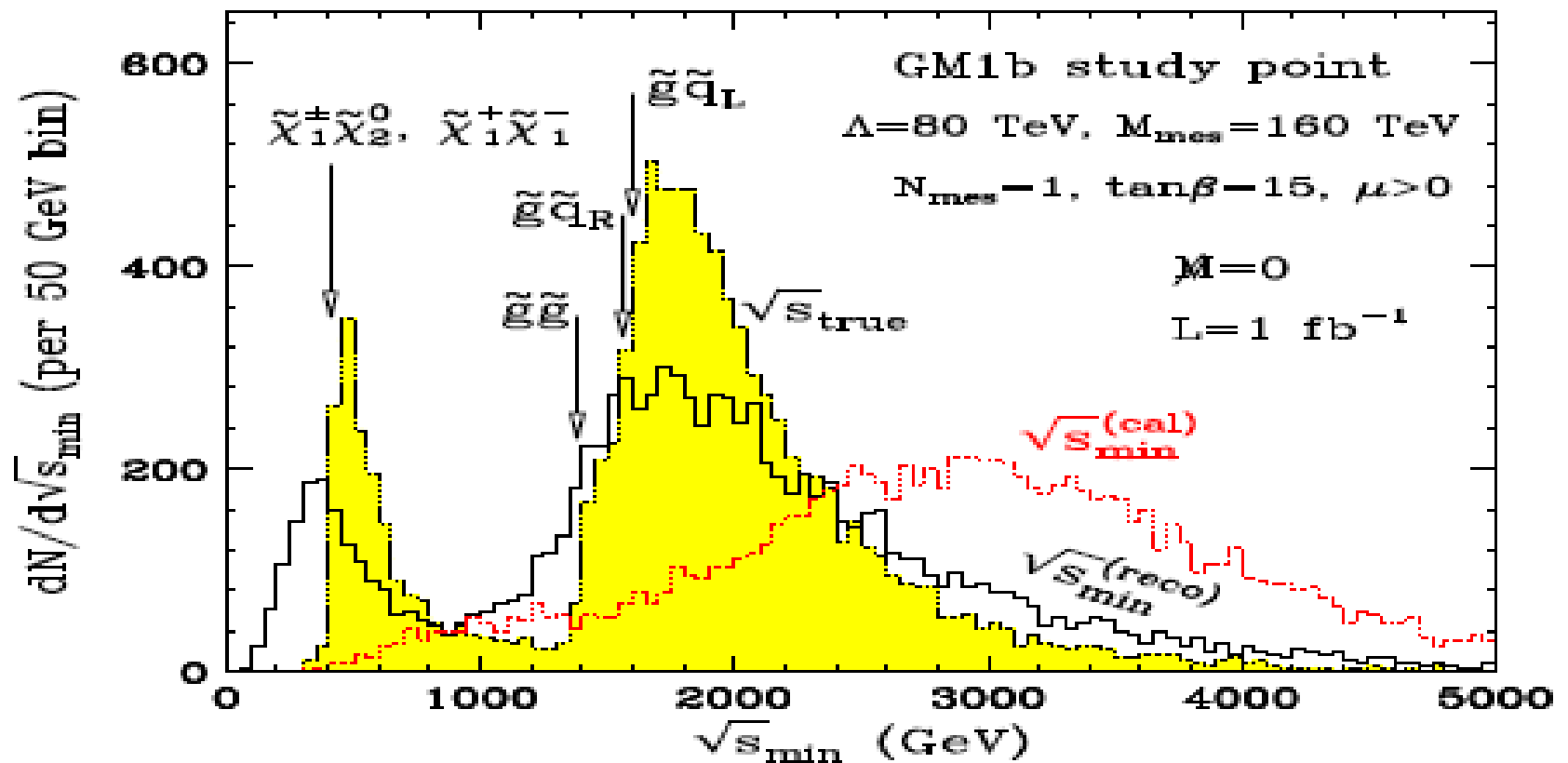
- identify the $N_1 N_1$ threshold from the 2 photon subsystem



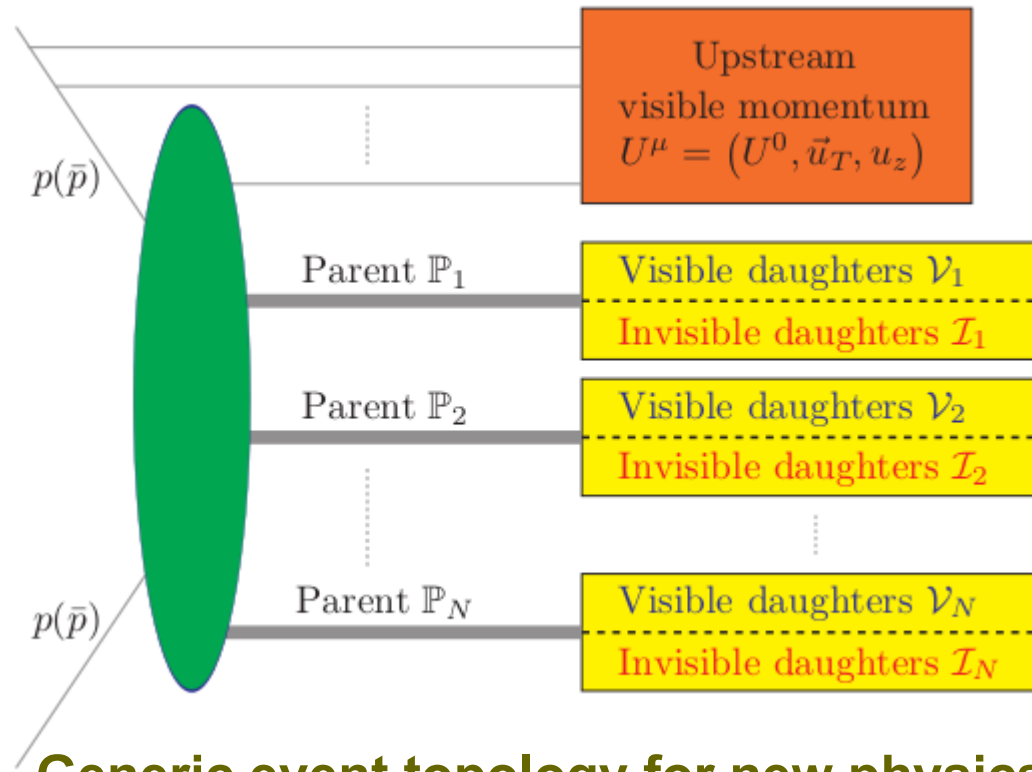
pk, Kong, Matchev, Park'10

$\sqrt{\hat{s}_{min}}$: Inclusive SUSY production

- The peak of $\sqrt{\hat{s}_{min}}$ locate the thresholds for individual dominant production sub-process
- GMSB study-point - GM1b : EW and strong productions



Event Partitioning



Generic event topology for new physics

**Constraint in
Transverse Projection**

$$\sum_{i=1}^{N_{\mathcal{I}}} \vec{q}_{iT} = \vec{p}_T^\# \equiv -\vec{u}_T - \sum_{i=1}^{N_{\mathcal{V}}} \vec{p}_{iT}.$$

Refine Transversification

Separate operations:

1. Partitioning & Summation of the mom-vec of the daughters [N]
2. Projecting into the transverse plane.
3. 2nd projection in to the transverse plane?
4. Minimisation at the end

Transverse Projection : Which way?

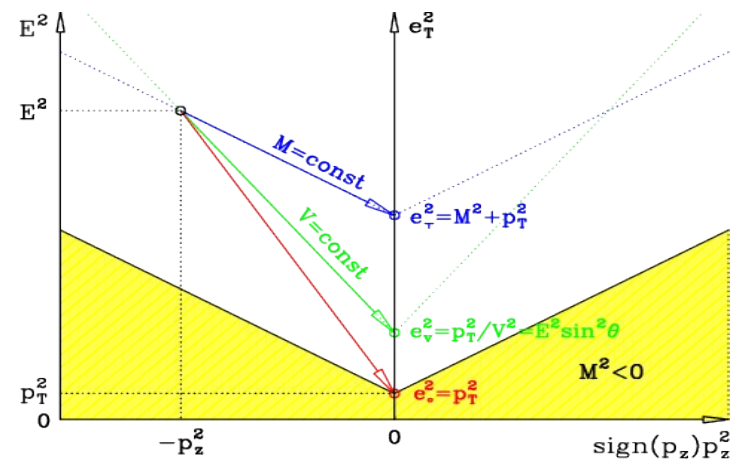
Mass-preserving "T"	Speed-preserving "V"	Massless "o"
---------------------	----------------------	--------------

Hierarchy:

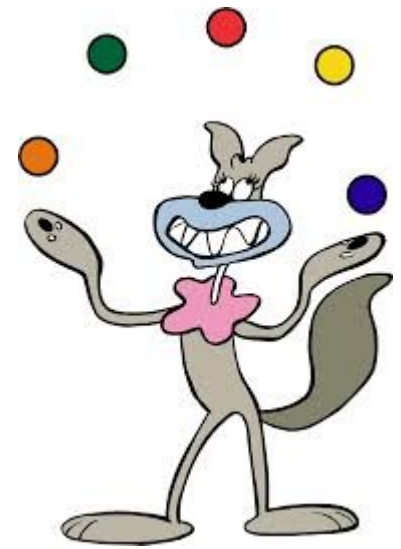
$$M = m_T \geq m_V \geq m_0 = 0.$$

&

$$E \geq e_T \geq e_V \geq e_0 = p_T.$$



Q. Separate operations: when and how ?



- (Partitioning & Summing) over visible momentums :

When and Which way – $N = 1, 2, \dots ?$

- Projecting into transverse plane : Y/N

If Y: When and Which way – $T, V, o ?$

- Second Projection : Y/N

If Y: Which way – $T, V, o ?$

- Minimization at the end.
$$\sum_{i=1}^{N_T} \vec{q}_{iT} = \vec{p}_T \equiv -\vec{u}_T - \sum_{i=1}^{N_V} \vec{p}_{iT}.$$

$$M_N, \quad M_{NT}, M_{NV}, M_{N0}, \quad M_{TN}, M_{VN}, M_{0N},$$

$$M_{NT\tau}: 27 \left(3 \text{ for } N \times 3 \text{ types of } T \times 3 \text{ types of } \tau \right)$$

How existing variables fit into

Existing variable	$N = 1$				$N = 2$	
	$M_1(\mathbb{M}_1) = M_{1\top}(\mathbb{M}_1)$	$M_{\top 1}(\mathbb{M}_1)$	M_{o1}	M_{1o}	$M_2(\mathbb{M}_a) = M_{2\top}(\mathbb{M}_a)$	$M_{2\top\perp}(\mathbb{M}_a)$
$2\phi_T = 2\hat{\phi}_T$				$u_T \rightarrow 0$		
m_{eff}		$\mathbb{M}_1 \rightarrow 0, u_T \rightarrow 0$	$u_T \rightarrow 0$			
$\sqrt{\hat{s}_{min}^{(sub)}}(\mathbb{M}_1)$	\checkmark					
$\sqrt{\hat{s}_{min}}(\mathbb{M}_1)$	$u_T \rightarrow 0$					
$m_{Tev}(M_e, M_\nu)$	\checkmark	\checkmark	$M_e, M_\nu \rightarrow 0$	$M_e, M_\nu \rightarrow 0$		
$M_{T,ZZ}(M_Z)$	\checkmark	\checkmark				
$M_{C,WW}$	$\mathbb{M}_1 \rightarrow 0$					
m_T^{true}	$\mathbb{M}_1 \rightarrow 0$					
$m_{T2}(\mathbb{M}_a)$					\checkmark	
$m_{T2\perp}(\mathbb{M}_a)$						\checkmark

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Guide to transverse projections and mass-constraining variables

A. J. Barr,¹ T. J. Khoo,² P. Konar,³ K. Kong,⁴ C. G. Lester,² K. T. Matchev,⁵ and M. Park⁵

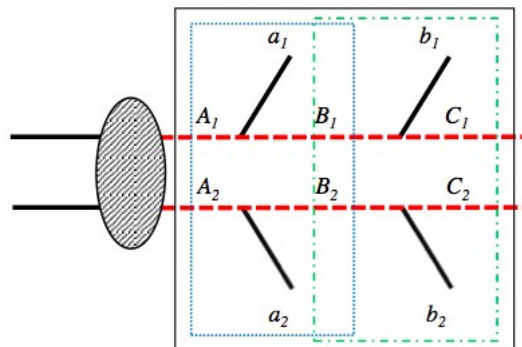
Some more recent works

❖ M2 variables, utility and topology

Cho, Gainer, Kim, Matchev, Moortgat, Pape, Park '14

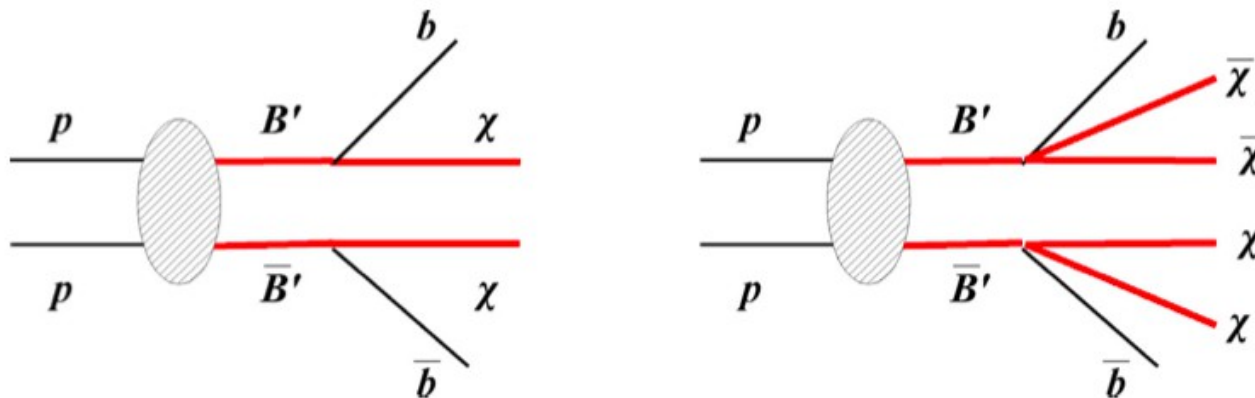
- Analogue to M_{T2} :

$$M_2(\tilde{m}) \equiv \min_{\vec{q}_1, \vec{q}_2} \{ \max [M_{P_1}(\vec{q}_1, \tilde{m}), M_{P_2}(\vec{q}_2, \tilde{m})] \}$$
- Based on different subsystem and using additional constraints from equality of “mother”, “Relative” variables like M_{2xx} , M_{2cx} , M_{2xc} , M_{2cc} are created
- Minimization over all components of “q”
- Sharper end point and test on topology informations.



Some more recent works

- ❖ **Dark Matter stabilization symmetry & Counting DM particles**
Agashe et al, '12, '13; Giudice, Gripaio, Mahbubani '12
- Peak of “visible” energy distribution, M_T and M_{T2} distribution.



- ❖ **Significance Variables**

Nachmana, Lester '13

- Includes the event by event resolution of kinematic variable
- Used to improve the analysis using M_T and M_{T2} as discrimination variable
- ❖ Apology that I could not add many more interesting works.

Summary

- Exciting time to cross-check the effectiveness new techniques with large amount LHC data.
- Compelling evidence for cold dark matter – turn for collider to find one.
- Motivates new model building : WIMP – our best bet.
- Mass (and spin) measurement one important step with signatures of new physics (and SM).
- Ideas and techniques developing fast for more generalised but precise measurements. CMS and ATLAS working closely to implement some of these ideas.
- Stay tuned with latest tricks in studying missing energy events.



Thank You